Multigap nodeless superconductivity in FeSe_x: Evidence from quasiparticle heat transport

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(Received 28 June 2009; revised manuscript received 12 July 2009; published 31 July 2009)

The in-plane thermal conductivity κ of the iron selenide superconductor FeSe_x (T_c =8.8 K) was measured down to 120 mK and up to 14.5 T (\approx 3/4 H_{c_2}). In zero field, the residual linear term κ_0/T at $T \rightarrow 0$ is only about 16 μ W K⁻² cm⁻¹, less than 4% of its normal-state value. Such a small κ_0/T does not support the existence of nodes in the superconducting gap. More importantly, the field dependence of κ_0/T in FeSe_x is very similar to that in NbSe₂, a typical multigap *s*-wave superconductor. We consider our data as strong evidence for multigap nodeless (at least in *ab* plane) superconductivity in FeSe_x. This kind of superconducting gap structure may be generic for all Fe-based superconductors.

DOI: 10.1103/PhysRevB.80.024518

PACS number(s): 74.25.Fy, 74.25.Op, 74.25.Jb

I. INTRODUCTION

Just as CuO plane is the basic building block of high- T_c cuprate superconductors, FeAs layer is the basic structure of the newly discovered FeAs-based high- T_c superconductors.^{1–7} The FeAs-layer consists of a Fe square planar sheet tetrahedrally coordinated by As. However, unlike the rigid CuO plane in cuprates, partial substitution of Fe by Co or Ni, or As by P within the FeAs-layer can effectively induce superconductivity.^{8–12} In this sense, the discovery of superconductivity in binary FeSe_r ($T_c \approx 8$ K) is of great interests since it only contains the superconducting FeSe layer which has identical structure as FeAs layer, and the Se deficiency may cause the superconductivity.¹³ More remarkably, the onset T_c can be enhanced to as high as 37 K for FeSe_x under high pressure,¹⁴⁻¹⁶ which further implies that superconductivity in FeSe_x may have the same mechanism as in FeAs-based superconductors.

For this new family of high- T_c superconductors, the pairing symmetry of its superconducting gap is a key to understand the mechanism of superconductivity. Extensive experimental and theoretical work have been done to address this important issue for FeAs-based superconductors (for a theoretical review, see Ref. 17; for an experimental review, see Ref. 18). Although there is still no consensus, more and more evidences point to multigap nodeless superconductivity, possibly an unconventional s^{\pm} paring mediated by antiferromagnetic fluctuations.¹⁹ For the prototype $FeSe_x$ superconductor, however, there were very few experiments to study the superconducting gap structure. This is due to its relatively lower T_c and lack of sizable high-quality single crystals.^{20,21} The measurements of in-plane magnetic penetration depth for polycrystal FeSe_{0.85} are in favor of anisotropic s-wave superconducting gap or two gaps (s+s).²² To clarify this important issue, more experimental work are needed for $FeSe_x$ superconductor.

Low-temperature thermal-conductivity measurement is a powerful tool to study the superconducting gap structure.²³ The field dependence of the residual thermal conductivity κ_0/T for BaNi₂As₂ (T_c =0.7 K) is consistent with a dirty fully gapped superconductivity.²⁴ For Ba_{1-x}K_xFe₂As₂

 $(T_c \simeq 30 \text{ K})$ and BaFe_{1.9}Ni_{0.1}As₂ $(T_c = 20.3 \text{ K})$, a negligible κ_0/T was found in zero field, indicating a full superconducting gap.^{25,26} However, $\kappa(T)$ was only measured in magnetic fields up to $\sim H_{c_2}/4$ (H=15 T), thus, cannot show clearly whether the superconductivity has multigap character in FeAs-based superconductors.^{25,26}

In this paper, we measure the in-plane thermal conductivity κ of a FeSe_x single crystal with T_c =8.8 K down to 120 mK and up to 14.5 T ($\approx 3/4H_{c_2}$) to probe its superconducting gap structure. In zero field, κ_0/T is about 16 μ W K⁻² cm⁻¹, less than 4% of its normal-state value. Such a small κ_0/T should not come from the nodal quasiparticle contribution. It may simply result from the slight overestimation when doing extrapolation, due to the lack of lower temperature data. The field dependence of κ_0/T is very similar to that in multigap *s*-wave superconductor NbSe₂. Based on our data, it is evident that FeSe_x is a multigap nodeless (at least in *ab* plane) superconductor.

II. EXPERIMENT

FeSe_x single crystals with nominal formula FeSe_{0.82} were grown via a vapor self-transport method.²¹ The *ab*-plane dimensions of as-grown crystals ranges from a few hundred μ m to 1 mm. Energy dispersive of x-ray (EDX) microanalysis (Hitachi S-4800) show that the actual Fe:Se ratio is very close to 1:1 in our FeSe_x single crystals. The nominal formula FeSe_{0.82} was used in the initial work by Hsu *et al.*¹³ However, the actual superconducting phase was later determined to be FeSe_{0.99±0.02} in Ref. 27 and FeSe_{0.974±0.005} in Ref. 28. Therefore the EDX result of our FeSe_x single crystals is consistent with these two later reports.

The ac susceptibility was measured in a Quantum Design Physical Property Measurement System (PPMS) with a modulation field of 10 Oe at 10 kHz. An as-grown single crystal with dimensions 1.0×0.40 mm² in the plane and 190 μ m thickness along the *c* axis was selected for transport study. Contacts were made directly on the sample surfaces with silver paint, which were used for both resistivity and thermal-conductivity measurements. The resistivity was measured by the standard four-probe method, using a low-



FIG. 1. (Color online) (a) In-plane resistivity $\rho(T)$ of FeSe_x single crystal in H=0 and 14.5 T magnetic fields along the *c* axis. The solid line is a linear fit of $\rho(T)$ from 8 to 30 K, which gives the residual resistivity $\rho_0=57.9 \ \mu\Omega$ cm in H=14.5 T. (b) The real part of ac susceptibility.

frequency ac resistance bridge (Lakeshore 370) with an excitation current I=1 mA. The typical contact resistance is a few ohms at room temperature and 1.5 K, which is not as good as that on Ba_{1-x}K_xFe₂As₂ and BaFe_{1.9}Ni_{0.1}As₂ single crystals.^{25,26} In-plane thermal conductivity was measured in a dilution refrigerator using a standard one-heater-two-thermometer steady-state technique.²⁹ Due to the small size of the sample and the nonideal contacts, good thermalization between sample and the two RuO₂ thermometers can only be achieved down to 120 mK. Magnetic fields were applied along the *c* axis and perpendicular to the heat current. To ensure a homogeneous field distribution in the sample, all fields were applied at temperature above T_c .

III. RESULTS AND DISCUSSION

Figure 1(a) shows the in-plane resistivity of FeSe_x single crystal in H=0 and 14.5 T magnetic fields. The middle point of the resistive transition is at $T_c=8.8$ K in zero field. The 10%–90% transition width of our crystal is as broad as the powder sample,¹³ which has been noticed in Ref. 21. Above T_c , $\rho(T)$ manifests a very good linear dependence up to 80 K, similar to the powder sample.¹³ A linear fit of $\rho(T)$ gives the residual resistivity $\rho_0=57.9$ $\mu\Omega$ cm in H=14.5 T, which is about 1/4 the value of powder sample.¹³

To estimate the upper critical field $H_{c_2}(0)$ which completely suppresses the resistive transition, we define $T_c(\text{onset})$ at the temperature where $\rho(T)$ deviates from the linear dependence, and get $T_c(\text{onset})=11.9$ and 6.3 K for H=0 and 14.5 T, respectively. Using the relationship $H_{c_2}/H_{c_2}(0)=1-[T/T_c(0)]^2$, we get $H_{c_2}(0)=20.1$ T. Note that $H_{c_2}(0)=16.3$ T was estimated for the powder sample, in which T_c was defined at the middle point of the transition.¹³



FIG. 2. (Color online) Temperature dependence of the in-plane thermal conductivity for FeSe_x single crystal in zero field. The solid line represents a fit of the data to $\kappa/T=a+bT^{\alpha-1}$. This gives the residual linear term $\kappa_0/T=16\pm 2 \ \mu W \ K^{-2} \ cm^{-1}$.

In Fig. 1(b), the real part of ac susceptibility for FeSe_x single crystal is plotted. The positive ferromagnetic background has been attributed to the existence of Fe impurity in the FeSe_x powder sample.¹³ However, no iron, iron oxide, or iron silicide impurities were detected in our crystals;²¹ therefore the ferromagnetic background likely results from the magnetic Fe cluster promoted by Se vacancies.³⁰

Figure 2 shows the temperature dependence of the inplane thermal conductivity for FeSe_x in zero field. To extrapolate the residual linear term κ_0/T , we fit the data to $\kappa/T=a+bT^{\alpha-1}$,^{29,31} where aT and bT^{α} represent electronic and phonon contributions, respectively. In Fig. 2, the data from 120 mK to 0.7 K can be fitted (the solid line) and gives $\kappa_0/T=16\pm 2 \ \mu\text{W} \text{ K}^{-2} \text{ cm}^{-1}$, with $\alpha=2.47$.

Such a value of κ_0/T is slightly larger than the experimental error bar $\pm 5^{\circ} \mu W K^{-2} cm^{-1}$.³¹ However, it is still fairly small, less than 4% of the normal-state Wiedemann-Franz law expectation $\kappa_{N0}/T = L_0/\rho_0 = 0.423 \text{ mW K}^{-2} \text{ cm}^{-1}$, with $L_0 = 2.45 \times 10^{-8} \text{ W } \Omega \text{ K}^{-2}$ and $\rho_0 = 57.9 \mu \Omega \text{ cm}$. For unconventional superconductors with nodes in the superconducting gap, a substantial κ_0/T in zero field contributed by the nodal quasiparticles has been found.^{32,33} For example, for overdoped d-wave cuprate superconductor Tl2201 with $T_c = 15$ K, $\kappa_0/T = 1.41$ mW K⁻² cm⁻¹, about 36% $\kappa_{N0}/T.^{32}$ For *p*-wave superconductor Sr_2RuO_4 with $T_c=1.5$ K, $\kappa_0/T = 17 \text{ mW K}^{-2} \text{ cm}^{-1}$, more than 9% κ_{N0}/T for the best sample.³³ We also note that κ_0/T in zero field are all negligible in closely related superconductors BaNi2As2, $Ba_{1-x}K_xFe_2As_2$, and $BaFe_{1,9}Ni_{0,1}As_2$.^{24–26} Therefore, it is unlikely that $\kappa_0/T = 16 \pm 2 \ \mu W \ K^{-2} \ cm^{-1}$ in FeSe_x single crystal comes from the nodal quasiparticle contribution. Since no impurity phases were detected, such a small κ_0/T may simply result from the slight overestimation when doing extrapolation, due to the lack of experimental data below 120 mK.

Below we turn to the field dependence of κ_0/T in FeSe_x. Figure 3 shows the low-temperature thermal conductivity of FeSe_x in magnetic fields applied along the *c* axis (*H*=0, 1, 4,



FIG. 3. (Color online) Low-temperature thermal conductivity of FeSe_x in magnetic fields applied along the *c* axis (*H*=0, 1, 4, 9, and 14.5 T). The solid lines are $\kappa/T=a+bT^{\alpha-1}$ fits. For *H*=4, 9, and 14.5 T, the electronic contribution becomes more and more dominant and the data get less smooth, therefore α is fixed to 2.47. The dashed line is the normal-state Wiedemann-Franz law expectation at $T \rightarrow 0$, namely, L_0/ρ_0 , with L_0 the Lorenz number $2.45 \times 10^{-8} \text{ W } \Omega \text{ K}^{-2}$.

9, and 14.5 T). For H=1 T, the data is also fitted to $\kappa/T=a+bT^{\alpha-1}$, and gives $\kappa_0/T=47\pm 2$ μ W K⁻² cm⁻¹, with $\alpha=2.47$. For H=4, 9, and 14.5 T, the electronic contribution becomes more and more dominant and the data get less smooth, therefore α is fixed to 2.47 in the phonon term bT^{α} . From Fig. 3, even higher magnetic field is needed to increase κ/T to its normal-state value.

In Fig. 4, we put the normalized $\kappa_0/T(H)$ of FeSe_x together with the clean *s*-wave superconductor Nb,³⁴ the dirty *s*-wave superconducting alloy InBi,³⁵ the multiband *s*-wave superconductor NbSe₂,³⁶ and an overdoped sample of the



FIG. 4. (Color online) Normalized residual linear term κ_0/T of FeSe_x plotted as a function of H/H_{c_2} . Similar data of the clean *s*-wave superconductor Nb (Ref. 34), the dirty *s*-wave superconductor nbSe₂ (Ref. 35), the multiband *s*-wave superconductor NbSe₂ (Ref. 36), and an overdoped sample of the *d*-wave superconductor TI-2201 (Ref. 32) are also shown for comparison.

d-wave superconductor Tl-2201,³² plotted as a function of H/H_{c_2} . For a clean (like Nb) or dirty (like InBi) type-II *s*-wave superconductor with isotropic gap, κ_0/T should grow exponentially with field (above H_{c_1}). This usually gives negligible κ_0/T for field lower than $H_{c_2}/4$. For the *d*-wave superconductor Tl-2201, κ_0/T increases roughly proportional to \sqrt{H} at low field due to the Volovik effect.³⁷ By contrast, for multigap superconductors NbSe₂ and MgB₂,^{36,38} magnetic field will first suppress the superconductivity on the Fermi surface with smaller gap, and give distinct shape of $\kappa_0/T(H)$ curve, as seen in Fig. 4.

From Fig. 4, the $\kappa_0/T(H)$ of FeSe_x manifests almost identical behavior as that of multigap s-wave superconductor NbSe₂. For NbSe₂, the shape of $\kappa_0/T(H)$ has been quantitatively explained by multiband superconductivity, whereby the gap on the Γ band is approximately one third of the gap on the other two Fermi surfaces.³⁶ Therefore, we consider our data as strong evidence for multigap nodeless superconductivity in FeSe,, with the ratio of the large gap to small gap close to 3. Note that in the two-gap s+s-wave model to describe the in-plane penetration depth data, the magnitude of the two gaps are 1.60 and 0.38 meV, respectively.²² The ratio of these two gaps is about 4, in agreement with the value estimated from our thermal-conductivity results. Since point nodes along c axis do not contribute to in-plane transport, measurement along c axis has to be done to rule out this possibility in FeSe,.

So far, there is still no experiment to directly measure the superconducting gap in $Fe_{1+\nu}Te_{1-\nu}Se_{\nu}$ system. Density functional calculations show that the electronic band structure of FeS, FeSe, and FeTe are very similar to the FeAs-based superconductors.³⁹ In doped BaFe₂As₂, multigap nodeless superconductivity has been clearly demonstrated by angle-resolved photoemission spectroscopy (ARPES) experiments.^{40–42} For hole-doped Ba_{0.6}K_{0.4}Fe₂As₂ $(T_c=37 \text{ K})$, the average gap values $\Delta(0)$ for the two hole pockets (α and β) are 12.5 and 5.5 meV, respectively, while for the electron (γ and δ) pockets, the gap value is similar, about 12.5 meV.^{40,41} For electron-doped BaFe_{1.85}Co_{0.15}As₂ $(T_c=25.5 \text{ K})$, the average gap values $\Delta(0)$ of hole (β) and electron (γ and δ) pockets are 6.6 and 5.0 meV, respectively.⁴² The ratio of the large gap to small gap is 2.3 for Ba_{0.6}K_{0.4}Fe₂As₂. This may explain the linear increase of $\kappa_0/T(H)$ at low field in Ba_{1-x}K_xFe₂As₂, with a smaller slope than that in NbSe₂.²⁵ However, magnetic field was only applied up to $H_{c_2}/4$ for Ba_{1-x}K_xFe₂As₂ and the multigap character of $\kappa_0/T(\tilde{H})$ was not as clear as in NbSe₂ and our FeSe_x single crystal.

IV. SUMMARY

In summary, we have measured the low-temperature thermal conductivity of iron selenide superconductor FeSe_x to investigate its superconducting gap structure. A fairly small κ_0/T at zero field and the dramatic field dependence of κ_0/T give strong evidence for multigap nodeless (at least in *ab* plane) superconductivity in FeSe_x. Such a gap structure may be generic for all Fe-based superconductors. More experiments are needed to distinguish unconventional s^{\pm} wave DONG et al.

from the conventional *s*-wave superconductivity in this new family of high- T_c superconductors.

ACKNOWLEDGMENTS

This work is supported by the Natural Science Foundation of China, the Ministry of Science and Technology of China

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(National Basic Research Program No. 2009CB929203), Program for New Century Excellent Talents in University, and STCSM of China (Grants No. 08dj1400200 and No. 08PJ1402100). The work in Northern Illinois University was supported by the U.S. Department of Energy through Grant No. DE-FG02-06ER46334 and Contract No. DE-AC02-06CH11357.

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